

1.26 Referring to Fig. 1.7,

(a) if the pressure in the tank is 1.5 bar and atmospheric pressure is 1 bar, determine L , in m, for water with a density of 997 kg/m^3 as the manometer liquid. Let $g = 9.81 \text{ m/s}^2$.

(b) determine L , in cm, if the manometer liquid is mercury with a density of 13.59 g/cm^3 and the gas pressure is 1.3 bar. A barometer indicates the local atmospheric pressure is 750 mmHg. Let $g = 9.81 \text{ m/s}^2$.

KNOWN: A manometer is attached to a tank containing a gas.

FIND: L considering two different manometer liquids with associated gas pressures.

SCHEMATIC AND GIVEN DATA:

(a) $p_{\text{gas}} = 1.5 \text{ bar}$

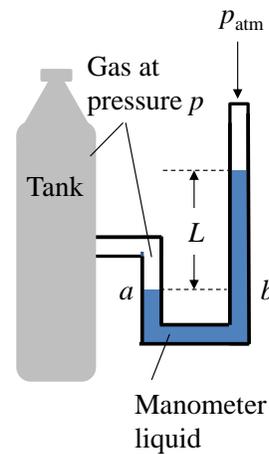
$p_{\text{atm}} = 1 \text{ bar}$

$\rho_{\text{water}} = 997 \text{ kg/m}^3$

(b) $p_{\text{gas}} = 1.3 \text{ bar}$

$p_{\text{atm}} = 750 \text{ mmHg}$

$\rho_{\text{mercury}} = 13.59 \text{ g/cm}^3$



ENGINEERING MODEL:

1. Local gravitational acceleration is 9.81 m/s^2 .

ANALYSIS:

(a) We have $p_a = p_{\text{gas}}$ and $p_a = p_b$. p_b is evaluated using Eq. 1.11. Collecting results,

$$p_{\text{gas}} = p_{\text{atm}} + \rho_w g L$$

where $\rho_w = 997 \text{ kg/m}^3$ and $g = 9.81 \text{ m/s}^2$.

Solving for L

$$L = \frac{p_{\text{gas}} - p_{\text{atm}}}{\rho_w g} = \frac{(1.5 - 1) \text{ bar}}{\left(997 \frac{\text{kg}}{\text{m}^3}\right) \left(9.81 \frac{\text{m}}{\text{s}^2}\right)} \left| \frac{10^5 \frac{\text{N}}{\text{m}^2}}{1 \text{ bar}} \right| \left| \frac{1 \frac{\text{kg} \cdot \text{m}}{\text{s}^2}}{1 \text{ N}} \right| = \underline{\underline{5.11 \text{ m}}}$$

(b) First solve for p_{atm} with $L = 750 \text{ mmHg}$ and $\rho_{\text{mercury}} = 13.59 \text{ g/cm}^3$.

$$p_{\text{atm}} = \rho_{\text{mercury}} g L$$

$$p_{\text{atm}} = \left(13.59 \frac{\text{g}}{\text{cm}^3} \right) \left| \frac{1 \text{ kg}}{10^3 \text{ g}} \right| \left| \frac{10^2 \text{ cm}}{1 \text{ m}} \right|^3 \left(9.81 \frac{\text{m}}{\text{s}^2} \right) (750 \text{ mmHg}) \left| \frac{1 \text{ m}}{10^3 \text{ mm}} \right| \left| \frac{1 \text{ N}}{1 \frac{\text{kg} \cdot \text{m}}{\text{s}^2}} \right| = 10^5 \text{ N/m}^2$$

Following the approach of part (a) and solving for L

$$L = \frac{p_{\text{gas}} - p_{\text{atm}}}{\rho_w g} = \frac{(1.3 - 1) \text{ bar}}{\left(13.59 \frac{\text{g}}{\text{cm}^3} \right) \left(9.81 \frac{\text{m}}{\text{s}^2} \right)} \left| \frac{10^3 \text{ g}}{1 \text{ kg}} \right| \left| \frac{1 \text{ m}}{10^2 \text{ cm}} \right|^3 \left| \frac{10^5 \frac{\text{N}}{\text{m}^2}}{1 \text{ bar}} \right| \left| \frac{1 \frac{\text{kg} \cdot \text{m}}{\text{s}^2}}{1 \text{ N}} \right| \left| \frac{100 \text{ cm}}{1 \text{ m}} \right| = \underline{\underline{22.5 \text{ cm}}}$$